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Grades K–12






Power Student Growth

Who understands the challenges teachers face better than you?

Meeting your needs is the first step to meeting the needs of students and supporting them as they tackle the standards and excel to higher levels of mathematical thinking.

Thanks to longstanding relationships with teachers and their insight, *Into Math™* and *Into AGA™* were developed by leading experts in the field of mathematics teaching and learning to ensure readiness and growth for each and every student.



Designed from the ground up, *Into Math* and *Into AGA* are the only solution built to monitor, predict, and accelerate growth for each and every student in Kindergarten to Grade 12.

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Unit 1: Count Sequence and Numbers to 5		
	Lessons	
Module 1—Represent Numbers to 5 with Objects	1.1	Represent 1 and 2
	1.2	Represent 3 and 4
	1.3	Represent 5
	1.4	Represent 0
	1.5	Ways to Make 5
	Lessons	
Module 2—Represent Numbers to 5 with a Written Numeral	2.1	Count and Write 0 and 1
	2.2	Count and Write 2 and 3
	2.3	Count and Write 4 and 5
	2.4	Count and Write Numbers to 5
	2.5	Count and Order to 5
	Lessons	
Module 3—Matching and Counting Numbers to 5	3.1	Identify a Greater Number of Objects Within 5
	3.2	Identify a Lesser Number of Objects Within 5
	3.3	Match Equal Groups of Objects Within 5
	3.4	Compare Groups Within 5 by Counting
	3.5	Compare Groups Within 5 by Matching
	3.6	Compare Numbers Within 5
	Lessons	
Module 4—Classify, Count, and Sort Objects	4.1	Classify and Count by Color
	4.2	Classify and Count by Shape
	4.3	Classify and Count by Size
	4.4	Classify, Count, and Sort by Count
	Lessons	
Module 5—Add To and Take From Within 5	5.1	Act Out Addition Problems Within 5
	5.2	Act Out Subtraction Problems Within 5
	5.3	Solve Add To Problems Within 5
	5.4	Solve Take From Problems Within 5
	5.5	Write Addition Equations Within 5
	5.6	Write Subtraction Equations Within 5
	5.7	Solve Result Unknown Word Problems Within 5

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	Lessons	
Module 6—Put Together and Take Apart Within 5	6.1	Represent Addition Problems Within 5 Using Objects and Drawings
	6.2	Represent Subtraction Problems Within 5 Using Objects and Drawings
	6.3	Solve Put Together Problems Within 5
	6.4	Solve Take Apart Problems Within 5
	6.5	Represent Addition Using Mental Images
	6.6	Represent Subtraction Using Mental Images
	6.7	Solve Word Problems Within 5
Unit 2: Count Sequence and Numbers to 10		
	Lessons	
Module 7—Represent Numbers 6 to 10 with Objects	7.1	Represent 6 and 7
	7.2	Represent 8 and 9
	7.3	Represent 10
	Lessons	
Module 8—Represent Numbers 6 to 10 with a Written Numeral	8.1	Count and Write 6 and 7
	8.2	Count and Write 8 and 9
	8.3	Count and Write 10
	8.4	Count and Order to 10
	Lessons	
Module 9—Use the Count Sequence to Count to 100	9.1	Count to 100 by Ones
	9.2	Count to 100 by Tens
	9.3	Count Forward From a Given Number
	Lessons	
Module 10—Compare Numbers to 10	10.1	Identify a Greater Number of Objects Within 10
	10.2	Identify a Lesser Number of Objects Within 10
	10.3	Match Equal Groups of Objects Within 10
	10.4	Compare Groups Within 10 by Counting
	10.5	Compare Groups Within 10 by Matching
	10.6	Compare Numbers Within 10



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	Lessons	
Module 11—Add To and Take From Within 10	11.1	Act Out Addition Problems Within 10
	11.2	Act Out Subtraction Problems Within 10
	11.3	Solve Add To Problems Within 10
	11.4	Solve Take From Problems Within 10
	11.5	Write Addition Equations Within 10
	11.6	Write Subtraction Equations Within 10
	11.7	Solve Result Unknown Word Problems Within 10
	Lessons	
Module 12—Put Together and Take Apart Within 10	12.1	Represent Addition Problems Within 10 Using Objects and Drawings
	12.2	Represent Subtraction Problems Within 10 Using Objects and Drawings
	12.3	Solve Put Together Problems Within 10
	12.4	Solve Take Apart Problems Within 10
	12.5	Solve Word Problems Within 10
	Lessons	
Module 13—Ways to Make Numbers to 10	13.1	Ways to Make 6 and 7
	13.2	Ways to Make 8
	13.3	Ways to Make 9
	13.4	Ways to Make 10
	13.5	Make 10 From a Given Number
Unit 3: Geometry		
	Lessons	
Module 14—Analyze and Compare Three-Dimensional Shapes	14.1	Identify and Describe Spheres
	14.2	Identify and Describe Cubes
	14.3	Identify and Describe Cylinders
	14.4	Identify and Describe Cones
	14.5	Build Shapes
	Lessons	
Module 15—Describe Positions of Objects	15.1	Use <i>Above</i> and <i>Below</i> to Describe Position
	15.2	Use <i>Next To</i> and <i>Beside</i> to Describe Position
	15.3	Use <i>In Front Of</i> and <i>Behind</i> to Describe Position

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	Lessons	
Module 16—Analyze and Compare Two-Dimensional Shapes	16.1	Identify and Describe Circles
	16.2	Identify and Describe Squares
	16.3	Identify and Describe Triangles
	16.4	Identify and Describe Rectangles
	16.5	Identify and Describe Hexagons
	16.6	Compose Simple Shapes
	16.7	Compare Two-Dimensional and Three-Dimensional Shapes
Unit 4: Number and Operations in Base Ten		
	Lessons	
Module 17—Place Value Foundations: Represent Numbers to 20	17.1	Compose Ten Ones and Some More Ones to 14
	17.2	Compose Ten Ones and Some More Ones to 15
	17.3	Compose Ten Ones and Some More Ones to 19
	17.4	Represent Numbers to 20
	Lessons	
Module 18— Place Value Foundations: Represent Numbers to 20 with a Written Numeral	18.1	Count and Write 11 to 14
	18.2	Count and Write 15
	18.3	Count and Write 16 to 19
	18.4	Count and Write 20
Unit 5: Measurement		
	Lessons	
Module 19—Length and Height	19.1	Describe Attributes of Length and Height
	19.2	Compare and Describe Lengths
	19.3	Compare and Describe Heights
	Lessons	
Module 20—Weight	20.1	Describe Attributes of Weight
	20.2	Compare and Describe Weights
	20.3	Describe More Than One Attribute of an Object



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Unit 1: Ways to Add and Subtract		
	Lessons	
Module 1—Addition Strategies	1.1	Represent Addition
	1.2	Count On
	1.3	Add 10 and More
	1.4	Make a 10 to Add
	1.5	Add Doubles
	1.6	Use Known Sums to Add
	1.7	Choose a Strategy to Add
	Lessons	
Module 2—Subtraction Strategies	2.1	Represent Subtraction
	2.2	Count Back
	2.3	Count On to Subtract
	2.4	Add to Subtract
	2.5	Use 10 to Subtract
	2.6	Choose a Strategy to Subtract
	Lessons	
Module 3—Properties of Operations	3.1	Represent Addition in Any Order
	3.2	Add in Any Order
	3.3	Represent Addition of 3 Numbers
	3.4	Add 3 Numbers
	3.5	Add 3 Numbers to Solve Problems
	3.6	Determine Equal and Not Equal
	3.7	Develop Fluency in Addition
	Lessons	
Module 4—Apply the Addition and Subtraction Relationship	4.1	Think Addition to Subtract
	4.2	Represent Related Facts
	4.3	Identify Related Facts
	4.4	Use Addition to Check Subtraction
	4.5	Use Subtraction to Find an Unknown Addend
	4.6	Solve for the Unknown Addend
	4.7	Develop Fluency in Subtraction

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Unit 2: Addition and Subtraction Situations and Data		
	Lessons	
Module 5—Understand Add To and Take From Problems	5.1	Represent Result Unknown Problems with Objects and Drawings
	5.2	Represent Change Unknown Problems with Objects and Drawings
	5.3	Represent Start Unknown Problems with Objects and Drawings
	5.4	Solve Add To and Take From Problems
	Lessons	
Module 6—Understand Put Together and Take Apart Problems	6.1	Represent Total Unknown Problems with Objects and Drawings
	6.2	Represent Both Addends Unknown Problems with Objects and Drawings
	6.3	Represent Addend Unknown Problems with Objects and Drawings
	6.4	Represent Total Unknown Problems with a Visual Model
	6.5	Represent Addend Unknown and Both Addends Unknown Problems with a Visual Model
	6.6	Solve Put Together and Take Apart Problems
	6.7	Solve Addition and Subtraction Problems
	Lessons	
Module 7—Understand Compare Problems	7.1	Represent Difference Unknown Problems with Objects and Drawings
	7.2	Represent Bigger Unknown Problems with Objects and Drawings
	7.3	Represent Smaller Unknown Problems with Objects and Drawings
	7.4	Represent Difference Unknown Problems with a Visual Model
	7.5	Represent Bigger Unknown and Smaller Unknown Problems with a Visual Model
	7.6	Use Strategies to Solve Compare Problems
	7.7	Solve Addition and Subtraction Situations
	Lessons	
Module 8—Data	8.1	Interpret Picture Graphs
	8.2	Represent Data with Picture Graphs
	8.3	Interpret Tally Charts
	8.4	Represent Data with Tally Charts
	8.5	Interpret Bar Graphs
	8.6	Represent Data with Bar Graphs
	8.7	Use Data to Solve Problems

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Unit 3: Numbers to 120		
	Lessons	
Module 9—Understand Place Value	9.1	Make Ten and Ones
	9.2	Understand Ten and Ones
	9.3	Make Tens
	Lessons	
Module 10—Count and Represent Numbers	10.1	Count to 120
	10.2	Represent Numbers as Tens and Ones with Objects
	10.3	Represent Numbers as Tens and Ones with Drawings
	10.4	Decompose Numbers in Different Ways
	10.5	Represent, Read, and Write Numbers from 100 to 110
	10.6	Represent, Read, and Write Numbers from 110 to 120
	Lessons	
Module 11—Compare Numbers	11.1	Understand Greater Than
	11.2	Understand Less Than
	11.3	Use Symbols to Compare
	11.4	Compare Numbers
Unit 4: Addition and Subtraction in Base Ten		
	Lessons	
Module 12—Understand Addition and Subtraction with Tens and Ones	12.1	Represent Adding Tens
	12.2	Represent Subtracting Tens
	12.3	Add or Subtract Tens
	12.4	Use a Hundred Chart to Add
	12.5	Represent Addition with Tens and Ones
	12.6	Represent Make Ten to Add
	12.7	Represent Make Ten to Add with a Visual Model
	12.8	Use Mental Math to Find 10 Less and 10 More
	Lessons	
Module 13—Two-Digit Addition and Subtraction	13.1	Use a Hundred Chart to Show Two-Digit Addition and Subtraction
	13.2	Understand and Explain Place Value Addition
	13.3	Understand and Explain Place Value Subtraction
	13.4	Solve Two-Digit Addition and Subtraction Problems
	13.5	Practice Facts to 20
	13.6	Practice Two-Digit Addition and Subtraction

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Unit 5: Geometry		
	Lessons	
Module 14—Three-Dimensional Shapes	14.1	Describe and Draw Three-Dimensional Shapes
	14.2	Compose Three-Dimensional Shapes
	14.3	Make New Three-Dimensional Shapes
	Lessons	
Module 15—Two-Dimensional Shapes	15.1	Sort Two-Dimensional Shapes by Attribute
	15.2	Describe and Draw Two-Dimensional Shapes
	15.3	Compose Two-Dimensional Shapes
	15.4	Identify Composed Shapes
	15.5	Make New Two-Dimensional Shapes
	Lessons	
Module 16—Fraction Foundations	16.1	Take Apart Two-Dimensional Shapes
	16.2	Identify Equal or Unequal Shares
	16.3	Partition Shapes into Halves
	16.4	Partition Shapes into Fourths
Unit 6: Measurement		
	Lessons	
Module 17—Measure Length	17.1	Order Length
	17.2	Use Indirect Measurement to Compare Length
	17.3	Use Nonstandard Units to Measure Length
	17.4	Make a Nonstandard Measuring Tool
	Lessons	
Module 18—Measure Time	18.1	Understand Time to the Hour
	18.2	Understand Time to the Half Hour
	18.3	Tell Time to the Hour and Half Hour
	18.4	Practice Time to the Hour and Half Hour



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Unit 1: Numbers to 20 and Data		
	Lessons	
Module 1—Fluency for Addition and Subtraction Within 20	1.1	Use Doubles Facts to Add
	1.2	Develop Fluency with Addition Using Strategies and Properties
	1.3	Relate Addition and Subtraction
	1.4	Develop Fluency with Subtraction Using Mental Strategies
	1.5	Use the Make a Ten Strategy to Add
	1.6	Use a Tens Fact to Subtract
	1.7	Add 3 Numbers Using Mental Strategies and Properties
	Lessons	
Module 2—Equal Groups	2.1	Identify Even and Odd Numbers
	2.2	Write Equations to Represent Even Numbers
	2.3	Represent Equal Groups
	2.4	Add to Find the Total Number of Objects in Arrays
	2.5	Practice with Arrays
	Lessons	
Module 3—Data	3.1	Collect and Record Data
	3.2	Interpret Picture Graphs
	3.3	Draw Picture Graphs to Represent Data
	3.4	Interpret Bar Graphs
	3.5	Draw Bar Graphs to Represent Data
Unit 2: Place Value		
	Lessons	
Module 4—Understand Place Value	4.1	Group Tens as Hundreds
	4.2	Understand Three-Digit Numbers
	4.3	Represent Three-Digit Numbers
	4.4	Represent Numbers with Hundreds, Tens, and Ones
	4.5	Place Value to 1,000
	Lessons	
Module 5—Read, Write, and Show Numbers to 1,000	5.1	Use Expanded Form
	5.2	Use Number Names
	5.3	Different Ways to Write Numbers
	5.4	Different Ways to Show Numbers
	5.5	Read, Write, and Show Numbers

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	Lessons	
Module 6—Use Place Value	6.1	Count Within 1,000
	6.2	Add and Subtract 10 or 100
	6.3	Identify and Extend Number Patterns
	6.4	Compare Three-Digit Numbers
	6.5	Use Symbols to Compare Numbers
Unit 3: Money and Time		
	Lessons	
Module 7—Coins	7.1	Relate Place Value to Coins
	7.2	Identify and Find the Value of Coins
	7.3	Compute the Value of Coin Combinations
	7.4	Show Amounts in Different Ways
	Lessons	
Module 8—Dollar Amounts	8.1	Relate the Value of Coins to One Dollar
	8.2	Compute the Value of Dollar Combinations
	8.3	Solve Problems Involving Money
	Lessons	
Module 9—Time	9.1	Tell and Write Time to 5 Minutes
	9.2	Different Ways to Tell and Write Time
	9.3	Practice Telling and Writing Time
	9.4	Tell and Write Time with a.m. and p.m.
Unit 4: Two-Digit Addition and Subtraction		
	Lessons	
Module 10—Addition and Subtraction Counting Strategies	10.1	Use a Hundred Chart
	10.2	Use a Number Line
	10.3	Use Counting Strategies
	Lessons	
Module 11—Addition and Subtraction Grouping Strategies	11.1	Decompose Ones to Add
	11.2	Decompose Ones to Subtract
	11.3	Decompose Numbers to Add
	11.4	Decompose Addends as Tens and Ones
	11.5	Decompose Numbers to Subtract

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	Lessons	
Module 12—Represent and Record Addition and Subtraction	12.1	Represent Regrouping for Addition
	12.2	Represent Regrouping for Subtraction
	12.3	Represent and Record Two-Digit Addition
	12.4	Represent and Record Two-Digit Subtraction
	12.5	Add Two-Digit Numbers
	12.6	Subtract Two-Digit Numbers
	Lessons	
Module 13—Develop Addition and Subtraction Fluency	13.1	Rewrite Addition Problems
	13.2	Rewrite Subtraction Problems
	13.3	Use Addition and a Number Line to Subtract
	13.4	Add 3 Two-Digit Numbers Using Strategies and Properties
	13.5	Add 4 Two-Digit Numbers Using Strategies and Properties
	Lessons	
Module 14—Algebra	14.1	Use Drawings to Represent Addition and Subtraction Situations
	14.2	Use Equations to Represent Addition and Subtraction Situations
	14.3	Use Drawings and Equations to Represent Two-Digit Addition
	14.4	Use Drawings and Equations to Represent Two-Digit Subtraction
	Lessons	
Module 15—Addition and Subtraction Word Problems	15.1	Solve Addition Word Problems
	15.2	Solve Subtraction Word Problems
	15.3	Solve Multistep Addition and Subtraction Problems
Unit 5: Three-Digit Addition and Subtraction		
	Lessons	
Module 16—Three-Digit Addition	16.1	Use Drawings to Represent Three-Digit Addition
	16.2	Decompose Three-Digit Addends
	16.3	Represent Regrouping for Addition
	16.4	Add Three-Digit Numbers
	Lessons	
Module 17—Three-Digit Subtraction	17.1	Represent Three-Digit Subtraction
	17.2	Represent Regrouping for Subtraction
	17.3	Subtract Three-Digit Numbers
	17.4	Represent Regrouping with Zeros
	17.5	Regrouping with Zeros
	17.6	Add and Subtract Three-Digit Numbers

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Unit 6: Measurement: Length		
	Lessons	
Module 18—Length in Inches, Feet, and Yards	18.1	Estimate Lengths Using Inches
	18.2	Make and Use a Ruler
	18.3	Measure to the Nearest Inch
	18.4	Make Line Plots to Show Measurement Data
	18.5	Estimate Lengths Using Feet
	18.6	Measure in Inches and Feet
	18.7	Measure to the Nearest Yard
	18.8	Choose Appropriate Tools
	Lessons	
Module 19—Length in Centimeters and Meters	19.1	Estimate Lengths Using Centimeters
	19.2	Measure to the Nearest Centimeter
	19.3	Estimate Lengths Using Meters
	19.4	Measure in Centimeters and Meters
	Lessons	
Module 20—Relate Addition and Subtraction to Length	20.1	Relate Inches to a Number Line
	20.2	Add and Subtract Lengths in Inches
	20.3	Relate Centimeters to a Number Line
	20.4	Add and Subtract Lengths in Centimeters
	20.5	Measure and Compare Lengths in Centimeters
Unit 7: Geometry and Fractions		
	Lessons	
Module 21—Two- and Three-Dimensional Shapes	21.1	Identify and Draw Three-Dimensional Shapes
	21.2	Identify and Draw Two-Dimensional Shapes
	21.3	Find and Count Angles in Two-Dimensional Shapes
	21.4	Sort Two-Dimensional Shapes by Sides and Angles
	Lessons	
Module 22—Understand Fractions	22.1	Partition Rectangles
	22.2	Identify and Describe Equal Shares
	22.3	Draw Equal Shares
	22.4	Show and Describe an Equal Share
	22.5	Different Ways to Show Equal Shares



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Unit 1: Understand Multiplication and Area		
	Lessons	
Module 1—Understand Multiplication	1.1	Count Equal Groups
	1.2	Relate Addition and Multiplication
	1.3	Represent Multiplication with Arrays
	1.4	Understand the Commutative Property of Multiplication
	1.5	Represent Multiplication with Number Lines
	1.6	Represent Multiplication with Bar Models
	Lessons	
Module 2—Relate Multiplication and Area	2.1	Understand Area by Counting Unit Squares
	2.2	Measure Area by Counting Unit Squares
	2.3	Relate Area to Addition and Multiplication
	2.4	Solve Problems with Area
	2.5	Find the Area of Combined Rectangles
Unit 2: Multiplication and Division		
	Lessons	
Module 3—Understand Multiplication Strategies	3.1	Multiply with 2 and 4
	3.2	Multiply with 5 and 10
	3.3	Multiply with 3 and 6
	Lessons	
Module 4—Apply Multiplication Properties as Strategies	4.1	Understand the Identity and Zero Properties of Multiplication
	4.2	Understand the Distributive Property
	4.3	Understand the Associative Property of Multiplication
	4.4	Multiply with 7
	4.5	Multiply with 8
	4.6	Multiply with 9
	4.7	Identify Number Patterns on the Multiplication Table
	Lessons	
Module 5—Multiplication with Multiples of 10	5.1	Use the Distributive Property
	5.2	Use the Associative Property of Multiplication
	5.3	Use Place Value Strategies to Multiply with Multiples of 10
	5.4	Multiply Multiples of 10 by 1-Digit

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	Lessons	
Module 6—Understand Division	6.1	Represent Division
	6.2	Separate Objects into Equal Groups
	6.3	Find the Number of Equal Groups
	6.4	Relate Subtraction and Division
	6.5	Represent Division with Arrays
	6.6	Represent Division with Bar Models
	6.7	Apply Division Rules for 1 and 0
	Lessons	
Module 7—Relate Multiplication and Division	7.1	Relate Multiplication and Division
	7.2	Write Related Facts
	7.3	Multiply and Divide with 2, 4, and 8
	7.4	Multiply and Divide with 5 and 10
	7.5	Multiply and Divide with 3 and 6
	7.6	Multiply and Divide with 7 and 9
	7.7	Build Fluency with Multiplication and Division
	Lessons	
Module 8—Apply Multiplication and Division	8.1	Identify and Extend Patterns
	8.2	Find Unknown Factors and Numbers
	8.3	Use Multiplication and Division to Solve Problem Situations
	8.4	Solve Two-Step Problems
	8.5	Practice with One- and Two-Step Problems
Unit 3: Addition and Subtraction Strategies and Applications		
	Lessons	
Module 9—Addition and Subtraction Strategies	9.1	Identify Number Patterns on the Addition Table
	9.2	Use Mental Math Strategies for Addition and Subtraction
	9.3	Use Properties to Add
	9.4	Use Mental Math to Assess Reasonableness
	9.5	Round to the Nearest Ten or Hundred
	9.6	Use Estimation with Sums and Differences



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	Lessons	
Module 10—Addition and Subtraction Within 1,000	10.1	Use Expanded Form to Add
	10.2	Use Place Value to Add
	10.3	Combine Place Values to Subtract
	10.4	Use Place Value to Subtract
	10.5	Choose a Strategy to Add or Subtract
	10.6	Model and Solve Two-Step Problems
	Lessons	
Module 11—Understand Perimeter	11.1	Describe Perimeter
	11.2	Find Perimeter
	11.3	Find Unknown Side Lengths
	11.4	Represent Rectangles with the Same Area and Different Perimeters
	11.5	Represent Rectangles with the Same Perimeter and Different Areas
	Lessons	
Module 12—Time Measurement and Intervals	12.1	Tell and Write Time to the Minute
	12.2	Use a.m. and p.m. to Describe Time
	12.3	Measure Time Intervals
	12.4	Find Start and End Times
	12.5	Solve Time Interval Problems
Unit 4: Fractions		
	Lessons	
Module 13—Understand Fractions as Numbers	13.1	Describe Equal Parts of a Whole
	13.2	Represent and Name Unit Fractions
	13.3	Represent and Name Fractions of a Whole
	13.4	Represent and Name Fractions on a Number Line
	13.5	Express Whole Numbers as Fractions
	13.6	Represent and Name Fractions Greater Than 1
	13.7	Use Fractions to Measure Lengths
	Lessons	
Module 14—Relate Shapes, Fractions, and Area	14.1	Relate Fractions and Area
	14.2	Partition Shapes into Equal Areas
	14.3	Use Unit Fractions to Describe Area
	Lessons	
Module 15—Compare Fractions	15.1	Compare Fractions Using Concrete and Visual Models
	15.2	Compare Fractions with the Same Denominator
	15.3	Compare Fractions with the Same Numerator
	15.4	Use Reasoning Strategies to Compare Fractions

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	Lessons	
Module 16—Understand Equivalent Fractions	16.1	Represent Equivalent Fractions with Smaller Parts
	16.2	Represent Equivalent Fractions with Larger Parts
	16.3	Recognize and Generate Equivalent Fractions
Unit 5: Measurement and Data		
	Lessons	
Module 17—Liquid Volume and Mass	17.1	Estimate and Measure Liquid Volume
	17.2	Estimate and Measure Mass
	17.3	Solve Problems About Liquid Volume and Mass
	Lessons	
Module 18—Represent and Interpret Data	18.1	Use Picture Graphs
	18.2	Make Picture Graphs
	18.3	Use Bar Graphs
	18.4	Make Bar Graphs
	18.5	Use Line Plots to Display Measurement Data
	18.6	Make Line Plots to Display Measurement Data
	18.7	Solve One- and Two-Step Problems Using Data
Unit 6: Geometry		
	Lessons	
Module 19—Define Two-Dimensional Shapes	19.1	Describe Shapes
	19.2	Describe Angles in Shapes
	19.3	Describe Sides of Shapes
	19.4	Define Quadrilaterals
	Lessons	
Module 20—Categorize Two-Dimensional Shapes	20.1	Draw Quadrilaterals
	20.2	Categorize Quadrilaterals
	20.3	Categorize Plane Shapes



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Unit 1: Place Value and Whole Number Operations		
	Lessons	
Module 1—Place Value of Whole Numbers	1.1	Understand Place Value Relationships
	1.2	Read and Write Numbers
	1.3	Regroup and Rename Numbers
	1.4	Compare and Order Numbers
	1.5	Use Place Value Understanding to Round Numbers
	Lessons	
Module 2—Addition and Subtraction of Whole Numbers	2.1	Add Whole Numbers and Assess Reasonableness
	2.2	Subtract Whole Numbers and Assess Reasonableness
	2.3	Use Addition and Subtraction to Solve Comparison Problems
	2.4	Apply the Perimeter Formula for Rectangles
Unit 2: Multiplication and Division Problems		
	Lessons	
Module 3—Interpret and Solve Problem Situations	3.1	Explore Multiplicative Comparisons
	3.2	Distinguish Between Multiplicative and Additive Comparisons
	3.3	Use Division to Solve Multiplicative Comparison Problems
	3.4	Use Comparisons to Solve Problem Situations
	3.5	Solve Multistep Problems with Multiplication and Division
	Lessons	
Module 4—Mental Math and Estimation Strategies	4.1	Explore Multiplication Patterns with Tens, Hundreds, and Thousands
	4.2	Explore Division Patterns with Tens, Hundreds, and Thousands
	4.3	Estimate Products by 1-Digit Numbers
	4.4	Estimate Quotients Using Compatible Numbers
	4.5	Use Mental Math Strategies for Multiplication and Division
	Lessons	
Module 5—Multiply by 1-Digit Numbers	5.1	Represent Multiplication
	5.2	Use Area Models and the Distributive Property to Multiply
	5.3	Multiply Using Expanded Form
	5.4	Multiply Using Partial Products
	5.5	Use Place Value to Multiply 2-Digit Numbers
	5.6	Multiply 3-Digit and 4-Digit Numbers
	5.7	Use Equations to Solve Multistep Problems

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	Lessons	
Module 6—Understand Division by 1-Digit Numbers	6.1	Represent Division
	6.2	Investigate Remainders
	6.3	Interpret Remainders
	6.4	Use Area Models and the Distributive Property to Divide
	6.5	Divide Using Repeated Subtraction
	6.6	Divide Using Partial Quotients
	Lessons	
Module 7—Divide by 1-Digit Numbers	7.1	Represent Division with Regrouping
	7.2	Use Place Value to Divide
	7.3	Divide by 1-Digit Numbers
	7.4	Solve Multistep Multiplication and Division Problems
Unit 3: Extend and Apply Multiplication		
	Lessons	
Module 8—Multiply by 2-Digit Numbers	8.1	Multiply with Tens
	8.2	Estimate Products
	8.3	Relate Area Models and Partial Products
	8.4	Multiply Using Partial Products
	8.5	Multiply with Regrouping
	8.6	Choose a Multiplication Strategy
	8.7	Solve Multistep Problems and Assess Reasonableness
	Lessons	
Module 9—Apply Multiplication to Area	9.1	Apply the Area Formula to Rectangles
	9.2	Find the Area of Combined Rectangles
	9.3	Find Unknown Measures
	9.4	Solve Area Problems
Unit 4: Fractions and Decimals		
	Lessons	
Module 10—Algebraic Thinking: Number Theory	10.1	Investigate Factors
	10.2	Identify Factors
	10.3	Generate Multiples Using Factors
	10.4	Identify Prime and Composite Numbers
	10.5	Generate and Analyze Number Patterns

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	Lessons	
Module 11—Fraction Equivalence and Comparison	11.1	Compare Fractions Using Visual Models
	11.2	Compare Fractions Using Benchmarks
	11.3	Explain Fraction Equivalence Using Visual Models
	11.4	Generate Equivalent Fractions
	11.5	Use Common Multiples to Write Equivalent Fractions
	11.6	Compare Fractions Using Common Numerators and Denominators
	11.7	Use Comparisons to Order Fractions
	Lessons	
Module 12—Relate Fractions and Decimals	12.1	Represent Tenths as Fractions and Decimals
	12.2	Represent Hundredths as Fractions and Decimals
	12.3	Identify Equivalent Fractions and Decimals
	12.4	Compare Decimals
	12.5	Relate Fractions, Decimals, and Money
	12.6	Solve Multistep Money Problems
	Lessons	
Module 13—Use Fractions to Understand Angles	13.1	Explore Lines, Rays, and Angles
	13.2	Explore Angles
	13.3	Relate Angles to Fractional Parts of a Circle
	13.4	Relate Degrees to Fractional Parts of a Circle
	13.5	Measure and Draw Angles Using a Protractor
	13.6	Join and Separate Angles
	13.7	Find Unknown Angle Measures
Unit 5: Operations with Fractions		
	Lessons	
Module 14—Understand Addition and Subtraction of Fractions with Like Denominators	14.1	Decompose Fractions into Sums
	14.2	Join Parts of the Same Whole
	14.3	Represent Addition of Fractions
	14.4	Separate Parts of the Same Whole
	14.5	Represent Subtraction of Fractions
	14.6	Add Fractional Parts of 10 and 100
	Lessons	
Module 15—Add and Subtract Fractions and Mixed Numbers with Like Denominators	15.1	Add and Subtract Fractions to Solve Problems
	15.2	Rename Fractions and Mixed Numbers
	15.3	Add and Subtract Mixed Numbers to Solve Problems
	15.4	Rename Mixed Numbers to Subtract
	15.5	Apply Properties of Addition to Add Fractions and Mixed Numbers
	15.6	Practice Solving Fraction Problems

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	Lessons	
Module 16—Multiply Fractions by Whole Numbers	16.1	Understand Multiples of Unit Fractions
	16.2	Find Multiples of Fractions
	16.3	Represent Multiplication of a Fraction by a Whole Number
	16.4	Solve Problems Using Multiplication of a Fraction or Mixed Number by a Whole Number
Unit 6: Two-Dimensional Figures and Symmetry		
	Lessons	
Module 17—Two-Dimensional Figures	17.1	Identify and Draw Perpendicular and Parallel Lines
	17.2	Identify and Classify Triangles by Angles
	17.3	Identify and Classify Triangles by Sides
	17.4	Identify and Classify Quadrilaterals
	17.5	Measure and Draw Angles of Two-Dimensional Figures
	Lessons	
Module 18—Symmetry and Patterns	18.1	Recognize Lines of Symmetry
	18.2	Identify and Draw Lines of Symmetry
	18.3	Generate and Identify Shape Patterns
Unit 7: Measurement, Data, and Time		
	Lessons	
Module 19—Relative Sizes of Customary Measurement Units	19.1	Identify Customary Measurement Benchmarks
	19.2	Compare Customary Units of Length
	19.3	Compare Customary Units of Weight
	19.4	Compare Customary Units of Liquid Volume
	19.5	Represent and Interpret Measurement Data in Line Plots
	Lessons	
Module 20—Relative Sizes of Metric Measurement Units	20.1	Identify Metric Measurement Benchmarks
	20.2	Compare Metric Units of Length
	20.3	Compare Metric Units of Mass and Liquid Volume
	20.4	Solve Problems Using Measurements
	Lessons	
Module 21—Solve Problems with Time and Measurement	21.1	Compare Units of Time
	21.2	Solve Problems Involving Elapsed Time
	21.3	Solve Problems Involving Start Time and End Time
	21.4	Practice with Mixed Measures

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Unit 1: Whole Numbers, Expressions, and Volume		
	Lessons	
Module 1—Whole Number Place Value and Multiplication	1.1	Recognize the 10 to 1 Relationship Among Place-Value Positions
	1.2	Use Powers of 10 and Exponents
	1.3	Use a Pattern to Multiply by Multiples of 10, 100, and 1,000
	1.4	Multiply by 1-Digit Numbers
	1.5	Multiply by Multi-Digit Numbers
	1.6	Develop Multiplication Fluency
	Lessons	
Module 2—Understand Division of Whole Numbers	2.1	Relate Multiplication to Division
	2.2	Represent Division with 2-Digit Divisors
	2.3	Estimate with 2-Digit Divisors
	2.4	Use Partial Quotients
	Lessons	
Module 3—Practice Division of Whole Numbers	3.1	Divide by 2-Digit Divisors
	3.2	Interpret the Remainder
	3.3	Adjust Quotients
	3.4	Practice with Division
	Lessons	
Module 4—Expressions	4.1	Write Numerical Expressions
	4.2	Interpret Numerical Expressions
	4.3	Evaluate Numerical Expressions
	4.4	Use Grouping Symbols
	Lessons	
Module 5—Volume	5.1	Use Unit Cubes to Build Solid Figures
	5.2	Understand Volume
	5.3	Estimate Volume
	5.4	Find Volume of Right Rectangular Prisms
	5.5	Apply Volume Formulas
	5.6	Find Volume of Composed Figures
Unit 2: Add and Subtract Fractions and Mixed Numbers		
	Lessons	
Module 6—Understand Addition and Subtraction of Fractions with Unlike Denominators	6.1	Represent Fraction Sums and Differences
	6.2	Represent Addition with Different-Sized Parts
	6.3	Represent Subtraction with Different-Sized Parts
	6.4	Rewrite Fractions with a Common Denominator

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	Lessons	
Module 7—Add and Subtract Fractions and Mixed Numbers with Unlike Denominators	7.1	Use Benchmarks and Number Sense to Estimate
	7.2	Assess Reasonableness of Fraction Sums and Differences
	7.3	Assess Reasonableness of Mixed Number Sums and Differences
	7.4	Rename Mixed Numbers to Subtract
	7.5	Apply Properties of Addition
	7.6	Practice Addition and Subtraction Using Equations
Unit 3: Multiply Fractions and Mixed Numbers		
	Lessons	
Module 8—Understand Multiplication of Fractions	8.1	Explore Groups of Equal Shares to Show Multiplication
	8.2	Represent Multiplication of Whole Numbers by Fractions
	8.3	Represent Multiplication with Unit Fractions
	8.4	Represent Multiplication of Fractions
	8.5	Use Representations of Area to Develop Procedures
	8.6	Interpret Fraction Multiplication as Scaling
	8.7	Multiply Fractions
	Lessons	
Module 9—Understand and Apply Multiplication of Mixed Numbers	9.1	Explore Area and Mixed Numbers
	9.2	Multiply Mixed Numbers
	9.3	Practice Multiplication with Fractions and Mixed Numbers
	9.4	Apply Fraction Multiplication to Find Area
Unit 4: Divide Fractions and Convert Customary Units		
	Lessons	
Module 10—Understand Division with Whole Numbers and Unit Fractions	10.1	Interpret a Fraction as Division
	10.2	Represent and Find the Size of Equal Parts
	10.3	Use Representations of Division of Unit Fractions by Whole Numbers
	10.4	Represent and Find the Number of Equal-Sized Parts
	10.5	Use Representations of Division of Whole Numbers by Unit Fractions



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	Lessons	
Module 11—Divide with Whole Numbers and Unit Fractions	11.1	Relate Multiplication and Division of Fractions
	11.2	Divide Whole Numbers by Unit Fractions
	11.3	Interpret and Solve Division of a Whole Number by a Unit Fraction
	11.4	Divide Unit Fractions by Whole Numbers
	11.5	Interpret and Solve Division of a Unit Fraction by a Whole Number
	11.6	Solve Division Problems Using Visual Models and Equations
	Lessons	
Module 12—Customary Measurement	12.1	Convert Customary Measurements
	12.2	Solve Multistep Customary Measurement Problems
	12.3	Represent and Interpret Measurement Data in Line Plots
	12.4	Convert Time and Find Elapsed Time
Unit 5: Add and Subtract Decimals		
	Lessons	
Module 13—Decimal Place Value	13.1	Understand Thousandths
	13.2	Read and Write Decimals to Thousandths
	13.3	Round Decimals
	13.4	Compare and Order Decimals
	Lessons	
Module 14—Add and Subtract Decimals	14.1	Represent Decimal Addition
	14.2	Represent Decimal Subtraction
	14.3	Assess Reasonableness of Sums and Differences
	14.4	Add Decimals
	14.5	Subtract Decimals
	14.6	Use Strategies and Reasoning to Add and Subtract
Unit 6: Multiply Decimals		
	Lessons	
Module 15—Multiply Decimals and Whole Numbers	15.1	Understand Decimal Multiplication Patterns
	15.2	Represent Multiplication with Decimals and Whole Numbers
	15.3	Assess Reasonableness of Products
	15.4	Multiply Decimals by 1-Digit Whole Numbers
	15.5	Multiply Decimals by 2-Digit Whole Numbers
	15.6	Solve Problems Using Bar Models

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	Lessons	
Module 16—Multiply Decimals	16.1	Represent Decimal Multiplication
	16.2	Multiply Decimals
	16.3	Multiply Decimals with Zeros in the Product
Unit 7: Divide Decimals and Convert Metric Units		
	Lessons	
Module 17—Divide Decimals	17.1	Understand Decimal Division Patterns
	17.2	Represent Division of Decimals by Whole Numbers
	17.3	Assess Reasonableness of Quotients
	17.4	Divide Decimals by Whole Numbers
	17.5	Represent Decimal Division
	17.6	Divide Decimals
	17.7	Write Zeros in the Dividend
	Lessons	
Module 18—Customary and Metric Measurement	18.1	Understand Metric Conversions
	18.2	Solve Customary and Metric Conversion Problems
	18.3	Solve Multistep Measurement Problems
Unit 8: Graphs, Patterns, and Geometry		
	Lessons	
Module 19—Graphs and Patterns	19.1	Describe a Coordinate System
	19.2	Understand Ordered Pairs
	19.3	Use Ordered Pairs to Represent Problems
	19.4	Generate and Identify Numerical Patterns
	19.5	Identify and Graph Relationships and Patterns
	Lessons	
Module 20—Classify Two-Dimensional Figures	20.1	Identify and Classify Polygons
	20.2	Classify and Organize Triangles
	20.3	Classify and Organize Quadrilaterals
	20.4	Use Venn Diagrams to Classify Two-Dimensional Figures



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Unit 1: Number Systems and Operations		
	Lessons	
Module 1—Integer Concepts	1.1	Identify and Interpret Integers
	1.2	Compare and Order Integers on a Number Line
	1.3	Find and Apply Absolute Value
	Lessons	
Module 2—Rational Number Concepts	2.1	Interpret Rational Numbers
	2.2	Compare Rational Numbers on a Number Line
	2.3	Find and Apply LCM and GCF
	2.4	Order Rational Numbers
	Lessons	
Module 3—Fraction Division	3.1	Understand Fraction Division
	3.2	Explore Division of Fractions with Unlike Denominators
	3.3	Explore Division of Mixed Numbers
	3.4	Practice and Apply Division of Fractions and Mixed Numbers
	3.5	Practice Fraction Operations
	Lessons	
Module 4—Fluency with Multi-Digit Decimal Operations	4.1	Add and Subtract Multi-Digit Decimals
	4.2	Multiply Multi-Digit Decimals
	4.3	Divide Multi-Digit Whole Numbers
	4.4	Divide Multi-Digit Decimals
	4.5	Apply Operations with Multi-Digit Decimals
Unit 2: Ratio and Rate Reasoning		
	Lessons	
Module 5—Ratios and Rates	5.1	Understand the Concept and Language of Ratios
	5.2	Represent Ratios and Rates with Tables and Graphs
	5.3	Compare Ratios and Rates
	5.4	Find and Apply Unit Rates
	5.5	Solve Ratio and Rate Problems Using Proportional Reasoning
	Lessons	
Module 6—Apply Ratios and Rates to Measurement	6.1	Use Ratio Reasoning with Circle Graphs
	6.2	Use Rate Reasoning to Convert Within Measurement Systems
	6.3	Use Rate Reasoning to Convert Between Measurement Systems
	Lessons	
Module 7—Understand and Apply Percent	7.1	Understand, Express, and Compare Percent Ratios
	7.2	Use Strategies to Find a Percent of a Quantity
	7.3	Solve a Variety of Percent Problems

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Unit 3: Expressions, Equations, and Inequalities		
	Lessons	
Module 8—Numerical and Algebraic Expressions	8.1	Understand and Apply Exponents
	8.2	Write and Evaluate Numerical Expressions for Situations
	8.3	Write Algebraic Expressions to Model Situations
	8.4	Interpret and Evaluate Algebraic Expressions
	8.5	Identify and Generate Equivalent Algebraic Expressions
	Lessons	
Module 9—Solve Problems Using Equations and Inequalities	9.1	Write Equations to Represent Situations
	9.2	Use Addition and Subtraction Equations to Solve Problems
	9.3	Use Multiplication and Division Equations to Solve Problems
	9.4	Use One-Step Equations to Solve a Variety of Problems
	9.5	Write and Graph Inequalities
	Lessons	
Module 10—Real-World Relationships Between Variables	10.1	Represent Equations in Tables and Graphs
	10.2	Write Equations from Verbal Descriptions
	10.3	Write Equations from Tables and Graphs
Unit 4: Relationships in Geometry		
	Lessons	
Module 11—Polygons on the Coordinate Plane	11.1	Graph Rational Numbers on the Coordinate Plane
	11.2	Graph Polygons on the Coordinate Plane
	11.3	Find Distance on the Coordinate Plane
	11.4	Find Perimeter and Area on the Coordinate Plane
	Lessons	
Module 12—Area of Triangles and Special Quadrilaterals	12.1	Develop and Use the Formula for Area of Parallelograms
	12.2	Develop and Use the Formula for Area of Triangles
	12.3	Develop and Use the Formula for Area of Trapezoids
	12.4	Find Area of Composite Figures
	Lessons	
Module 13—Surface Area and Volume	13.1	Explore Nets and Surface Area
	13.2	Find Volume of Rectangular Prisms
	13.3	Solve Volume Problems



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Unit 5: Data Collection and Analysis		
	Lessons	
Module 14—Data Collection and Displays	14.1	Explore Statistical Data Collection
	14.2	Display Data in Dot Plots
	14.3	Make Histograms and Frequency Tables
	Lessons	
Module 15—Measures of Center	15.1	Explore Mean as Fair Share
	15.2	Find Measures of Center
	15.3	Choose a Measure of Center
	Lessons	
Module 16—Variability and Data Distribution	16.1	Explore Patterns of Data
	16.2	Display Data in Box Plots
	16.3	Find Mean Absolute Deviation
	16.4	Explore Measures of Variability
	16.5	Describe Distributions

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Unit 1: Proportional Relationships		
	Lessons	
Module 1—Identify and Represent Proportional Relationships	1.1	Explore Relationships
	1.2	Recognize Proportional Relationships in Tables
	1.3	Compute Unit Rates Involving Fractions
	1.4	Recognize Proportional Relationships in Graphs
	1.5	Use Proportional Relationships to Solve Rate Problems
	1.6	Practice Proportional Reasoning with Scale Drawings
	Lessons	
Module 2—Proportional Reasoning with Percents	2.1	Percent Change
	2.2	Markups and Discounts
	2.3	Taxes and Gratuities
	2.4	Commissions and Fees
	2.5	Simple Interest
Unit 2: Rational Number Operations		
	Lessons	
Module 3—Understand Addition and Subtraction of Rational Numbers	3.1	Add or Subtract a Positive Integer on a Number Line
	3.2	Add or Subtract a Negative Integer on a Number Line
	3.3	Use a Number Line to Add and Subtract Rational Numbers
	Lessons	
Module 4—Add and Subtract Rational Numbers	4.1	Compute Sums of Integers
	4.2	Compute Differences of Integers
	4.3	Compute Sums and Differences of Rational Numbers
	4.4	Apply Properties to Multi-Step Addition and Subtraction Problems
	Lessons	
Module 5—Multiply and Divide Rational Numbers	5.1	Understand Multiplication and Division of Rational Numbers
	5.2	Multiply Rational Numbers
	5.3	Write Fractions as Decimals and Divide Integers
	5.4	Multiply and Divide Rational Numbers in Context
	Lessons	
Module 6—Solve Multi-Step Problems Using Rational Numbers	6.1	Apply Properties and Strategies to Operate with Rational Numbers
	6.2	Estimate to Check Reasonableness
	6.3	Solve Multi-Step Problems with Rational Numbers in Context

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Unit 3: Model with Expressions, Equations, and Inequalities		
	Lessons	
Module 7—Solve Problems Using Expressions and Equations	7.1	Write Linear Expressions in Different Forms for Situations
	7.2	Add, Subtract, and Factor Linear Expressions with Rational Coefficients
	7.3	Write Two-Step Equations for Situations
	7.4	Apply Two-Step Equations to Solve Real-World Problems
	7.5	Apply Two-Step Equations to Find Angle Measures
	Lessons	
Module 8—Solve Problems Using Inequalities	8.1	Understand and Apply Properties to Solve One-Step Inequalities
	8.2	Write Two-Step Inequalities for Situations
	8.3	Apply Two-Step Inequalities to Solve Problems
Unit 4: Geometry		
	Lessons	
Module 9—Draw and Analyze Two-Dimensional Figures	9.1	Draw Circles and Other Figures
	9.2	Draw and Construct Triangles Given Side Lengths
	9.3	Draw and Construct Triangles Given Angle Measures
	9.4	Draw and Analyze Shapes to Solve Problems
	Lessons	
Module 10—Analyze Figures to Find Circumference and Area	10.1	Derive and Apply Formulas for Circumference
	10.2	Derive and Apply a Formula for the Area of a Circle
	10.3	Describe and Analyze Cross Sections of Circular Solids
	10.4	Areas of Composite Figures
	Lessons	
Module 11—Analyze Surface Area and Volume	11.1	Describe and Analyze Cross Sections of Prisms and Pyramids
	11.2	Derive and Apply Formulas for Surface Areas of Cubes and Right Prisms
	11.3	Derive and Apply a Formula for the Volume of a Right Prism
	11.4	Solve Multi-Step Problems with Surface Area and Volume
Unit 5: Sampling and Data Analysis		
	Lessons	
Module 12—Proportional Reasoning with Samples	12.1	Understand Representative Samples
	12.2	Make Inferences from a Random Sample
	12.3	Make Inferences from Repeated Random Samples

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	Lessons	
Module 13—Use Statistics and Graphs to Compare Data	13.1	Compare Center and Spread of Data Displayed in Dot Plots
	13.2	Compare Center and Spread of Data Displayed in Box Plots
	13.3	Compare Means Using Mean Absolute Deviation and Repeated Sampling
Unit 6: Probability		
	Lessons	
Module 14—Understand and Apply Experimental Probability	14.1	Understand Probability of an Event
	14.2	Find Experimental Probability of Simple Events
	14.3	Find Experimental Probability of Compound Events
	14.4	Use Experimental Probability and Proportional Reasoning to Make Predictions
	Lessons	
Module 15—Understand and Apply Theoretical Probability	15.1	Find Theoretical Probability of Simple Events
	15.2	Find Theoretical Probability of Compound Events
	15.3	Use Theoretical Probability and Proportional Reasoning to Make Predictions
	15.4	Conduct Simulations



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Unit 1: Transformational Geometry		
	Lessons	
Module 1—Transformations and Congruence	1.1	Investigate Transformations
	1.2	Explore Translations
	1.3	Explore Reflections
	1.4	Explore Rotations
	1.5	Understand and Recognize Congruent Figures
	Lessons	
Module 2—Transformations and Similarity	2.1	Investigate Reductions and Enlargements
	2.2	Explore Dilations
	2.3	Understand and Recognize Similar Figures
Unit 2: Linear Equations and Applications		
	Lessons	
Module 3—Solve Linear Equations	3.1	Solve Multi-Step Linear Equations
	3.2	Examine Special Cases
	3.3	Apply Linear Equations
	Lessons	
Module 4—Angle Relationships	4.1	Develop Angle Relationships for Triangles
	4.2	Investigate Angle-Angle Similarity
	4.3	Explore Parallel Lines Cut by a Transversal
Unit 3: Relationships and Functions		
	Lessons	
Module 5—Proportional Relationships	5.1	Explain Slope with Similar Triangles
	5.2	Derive $y = mx$
	5.3	Interpret and Graph Proportional Relationships
	5.4	Compare Proportional Relationships
	Lessons	
Module 6—Understand and Analyze Functions	6.1	Understand and Graph Functions
	6.2	Derive and Interpret $y = mx + b$
	6.3	Interpret Rate of Change and Initial Value
	6.4	Construct Functions
	6.5	Compare Functions
	6.6	Describe and Sketch Nonlinear Functions

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	Lessons	
Module 7—Systems of Linear Equations	7.1	Represent Systems by Graphing
	7.2	Solve Systems by Graphing
	7.3	Solve Systems by Substitution
	7.4	Solve Systems by Elimination
	7.5	Examine Special Systems
	7.6	Apply Systems of Equations
Unit 4: Statistics and Probability		
	Lessons	
Module 8—Scatter Plots	8.1	Construct Scatter Plots and Examine Association
	8.2	Draw and Analyze Trend Lines
	8.3	Interpret Linear Data in Context
	Lessons	
Module 9—Two-Way Tables	9.1	Construct and Interpret Two-Way Frequency Tables
	9.2	Construct Two-Way Relative Frequency Tables
	9.3	Interpret Two-Way Relative Frequency Tables
Unit 5: Real Numbers and the Pythagorean Theorem		
	Lessons	
Module 10—Real Numbers	10.1	Understand Rational and Irrational Numbers
	10.2	Investigate Roots
	10.3	Order Real Numbers
	Lessons	
Module 11—The Pythagorean Theorem	11.1	Prove the Pythagorean Theorem
	11.2	Prove the Converse of the Pythagorean Theorem
	11.3	Apply the Pythagorean Theorem
	11.4	Apply the Pythagorean Theorem in the Coordinate Plane
Unit 6: Exponents, Scientific Notation, and Volume		
	Lessons	
Module 12—Exponents and Scientific Notation	12.1	Know and Apply Properties of Exponents
	12.2	Understand Scientific Notation
	12.3	Compute with Scientific Notation
	Lessons	
Module 13—Volume	13.1	Find Volume of Cylinders
	13.2	Find Volume of Cones
	13.3	Find Volume of Spheres
	13.4	Apply Volume



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Unit 1: Real Numbers and Connections to Algebra		
	Lessons	
Module 1: Real Numbers and Real-World Quantities	1.1	Real Numbers
	1.2	Radicals and Rational Exponents
	1.3	Precision and Accuracy in Calculations
	Lessons	
Module 2: Linear Equations and Inequalities in One Variable	2.1	Write, Interpret, and Simplify Expressions
	2.2	Write and Solve Equations
	2.3	Rewrite Formulas and Solve Literal Equations
	2.4	Write and Solve Inequalities
	2.5	Write and Solve Compound Inequalities
Unit 2: Linear Equations in Two Variables		
	Lessons	
Module 3: Linear Equations in Two Variables	3.1	Linear Equations in Standard Form
	3.2	Slopes of Lines and Rates of Change
	Lessons	
Module 4: Linear Functions and Models	4.1	Relations and Functions
	4.2	Linear Functions
	4.3	Characteristics of Linear Functions
	4.4	Linear Models and Point-Slope Form
	Lessons	
Module 5: Relationships Among Linear Functions	5.1	Transform Graphs
	5.2	Transform Linear Functions
	5.3	Compare Linear Functions
	5.4	Inverses of Linear Functions
Unit 3: Build Linear Functions and Models		
	Lessons	
Module 6: Fit Linear Functions to Data	6.1	Scatter Plots, Correlation, and Fitted Lines
	6.2	Residuals and Best-Fit Lines
	Lessons	
Module 7: Discrete Linear Functions	7.1	Arithmetic Sequences Defined Recursively
	7.2	Arithmetic Sequences Defined Explicitly

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	Lessons	
Module 8: Piecewise-Defined Functions	8.1	Graph Piecewise-Defined Functions
	8.2	Graph Absolute Value Functions
	8.3	Absolute Value Equations and Inequalities
Unit 4: Linear Systems		
	Lessons	
Module 9: Systems of Linear Equations	9.1	Solve Linear Systems by Graphing
	9.2	Solve Linear Systems by Substitution
	9.3	Solve Linear Systems by Adding or Subtracting
	9.4	Solve Linear Systems by Multiplying First
	Lessons	
Module 10: Linear Inequalities	10.1	Linear Inequalities in Two Variables
	10.2	Graph Systems of Linear Inequalities
Unit 5: Functions and Equations		
	Lessons	
Module 11: Exponential Functions and Models	11.1	Exponential Growth Functions
	11.2	Exponential Decay Functions
	11.3	Exponential Models and Equations
	Lessons	
Module 12: Relationships Among Exponential Functions	12.1	Transform Exponential Functions
	12.2	Compare Exponential Functions
Unit 6: Build Exponential Functions and Models		
	Lessons	
Module 13: Fit Exponential Functions to Data	13.1	Scatter Plots and Fitted Exponential Curves
	13.2	Choose Between Linear and Exponential Models
	Lessons	
Module 14: Discrete Exponential Functions	14.1	Geometric Sequences Defined Recursively
	14.2	Geometric Sequences Defined Explicitly

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Unit 7: Polynomial Operations and Models		
	Lessons	
Module 15: Polynomial Multiplication	15.1	Multiply Monomials
	15.2	Multiply Monomials, Binomials, and Trinomials
	15.3	Special Products of Binomials
	Lessons	
Module 16: Polynomial Addition and Subtraction	16.1	Add and Subtract Polynomials
	16.2	Model with Polynomials
Unit 8: Quadratic Functions and Equations		
	Lessons	
Module 17: Use Graphing and Factoring to Solve Quadratic Equations	17.1	Solve Quadratic Equations by Graphing Quadratic Functions
	17.2	Solve Quadratic Equations by Factoring $x^2 + bx + c$
	17.3	Solve Quadratic Equations by Factoring $ax^2 + bx + c$
	17.4	Use Special Factoring Patterns to Solve Quadratic Equations
	Lessons	
Module 18: Use Square Roots to Solve Quadratic Equations	18.1	Solve Quadratic Equations by Taking Square Roots
	18.2	Solve Quadratic Equations by Completing the Square
	18.3	Use the Quadratic Formula to Solve Equations
	18.4	Choose a Method for Solving Quadratic Equations

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Unit 9: Functions and Models		
	Lessons	
Module 19: Build Quadratic Functions and Models	19.1	Quadratic Functions in Vertex Form
	19.2	Quadratic Functions in Standard Form
	19.3	Quadratic Functions in Intercept Form
	19.4	Compare Quadratic Functions and Models
	19.5	Scatter Plots and Fitted Quadratic Curves
	Lessons	
Module 20: Function Analysis	20.1	Choose Among Linear, Exponential, and Quadratic Models
	20.2	Perform Operations with Functions
	20.3	Solve Nonlinear Systems
	20.4	Cubic Functions
Unit 10: Data Analysis		
	Lessons	
Module 21: Categorical Data	21.1	Two-Way Frequency and Relative Frequency Tables
	21.2	Recognize Possible Associations Between Categorical Variables
	Lessons	
Module 22: Numerical Data	22.1	Data Distributions and Appropriate Statistics
	22.2	Compare Data Distributions



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Unit 1: The Essentials of Geometry		
	Lessons	
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	1.2	Define and Measure Angles
	1.3	Polygons and Figures in the Plane
	1.4	Length in the Coordinate Plane
	Lessons	
Module 2: Tools for Reasoning and Proof	2.1	Write Conditional Statements
	2.2	Use Inductive and Deductive Reasoning
	2.3	Write Proofs about Segments
	2.4	Write Proofs about Angles
Unit 2: Parallel and Perpendicular Lines		
	Lessons	
Module 3: Lines and Transversals	3.1	Parallel Lines Crossed by a Transversal
	3.2	Prove Lines Are Parallel
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Module 4: Lines on the Coordinate Plane	4.1	Slope and Equations of Parallel Lines
	4.2	Slope and Equations of Perpendicular Lines
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	Lessons	
Module 5: Transformations that Preserve Size and Shape	5.1	Define and Apply Translations
	5.2	Define and Apply Rotations
	5.3	Define and Apply Reflections
	5.4	Define and Apply Symmetry
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Module 6: Transformations that Change Size and Shape	6.1	Define and Apply Dilations and Stretches
	6.2	Apply Sequences of Transformations

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Module 7: Congruent Triangles and Polygons	7.1	Understand Congruent Figures
	7.2	Corresponding Parts of Congruent Figures
	7.3	Use Rigid Motions to Prove Figures Are Congruent
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Module 8: Triangle Congruence Criteria	8.1	Develop ASA Triangle Congruence
	8.2	Develop SAS Triangle Congruence
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	8.4	Develop AAS and HL Triangle Congruence
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Module 9: Properties of Triangles	9.1	Angles in Triangles
	9.2	Perpendicular Bisectors
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	9.4	Medians and Altitudes
	9.5	The Triangle Midsegment Theorem
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Module 10: Triangle Inequalities	10.1	Inequalities in One Triangle
	10.2	Inequalities in Two Triangles
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Module 11: Quadrilaterals and Polygons	11.1	Properties of Parallelograms
	11.2	Conditions for Parallelograms
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	11.4	Conditions for Rectangles, Rhombuses, Squares
	11.5	Properties and Conditions for Trapezoids and Kites

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	12.2	Develop AA Triangle Similarity
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	13.2	Sine and Cosine Ratios
	13.3	Special Right Triangles
	13.4	Modeling with Similar Right Triangles
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Module 14: Trigonometry with All Triangles	14.1	Law of Sines
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Module 15: Lines that Intersect Circles	15.1	Central Angles and Inscribed Angles
	15.2	Angles in Inscribed Quadrilaterals
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	20.2	Mutually Exclusive and Overlapping Events
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	2.2	Operations with Complex Numbers
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	9.2	Graph Logarithmic Functions
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	10.2	Solve Exponential Equations
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	15.2	Define and Evaluate the Basic Trigonometric Functions
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Module 16: Graph Trigonometric Functions	16.1	Graph Sine and Cosine Functions
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